

## ZOOM OPTICAL SYSTEM FOR THERMAL CAMERA IN OPTICAL RANGE 8-14 $\mu\text{m}$

Chi Toan DANG, Vratislav KREHEL, Michal MOZOLA

**Abstract:** Continuous infrared zoom systems with image quality and image stabilisation maintained throughout the workflow are increasingly being used. A long-wave infrared continuous zoom optical system with a 6x zoom ratio operating with an uncooled detector was designed. The optical system has a focal length from 37,5 mm to 225 mm, and the F/# is 1,5. The system includes 7 lenses with 3 even aspheres. The results show that the MTF function is very close to the diffraction limit curve over the entire focal range, proving that the system meets the specifications.

**Keywords:** Zoom optical system; Thermal infrared; Zoom ratio.

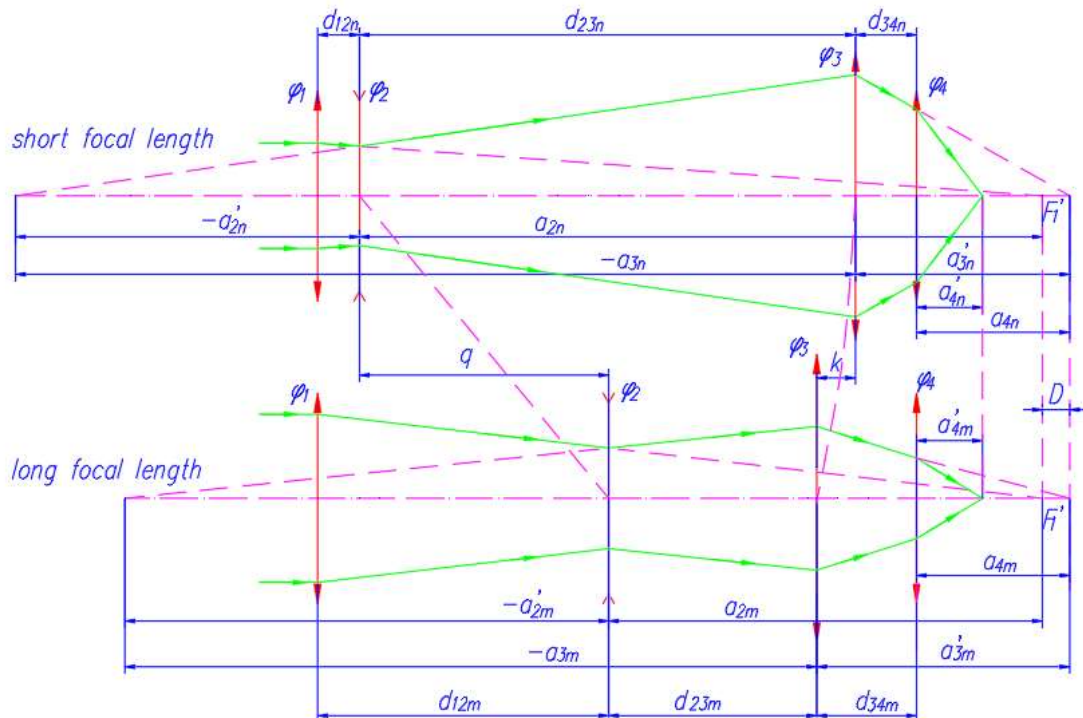
### 1 INTRODUCTION

The infrared zoom (IR) optical system is capable of detecting, tracking and continuously acquiring information, so with the development of the new generation of uncooled detectors, much more compact zoom thermal imaging devices were born [1, 2]. Because the IR zoom optical system has a continuously variable focal length, to ensure the image quality of the system in the entire focal range, image compensation must be calculated. The calculation of image compensation is usually based on two methods: optical compensation and mechanical compensation. According to the optical compensation method, the image plane can only be stabilised at a few different focal positions, so this method is suitable for designing optical systems with low zoom ratios. In contrast,

the mechanical compensation method ensures that the optical system changes focus continuously over a certain range and is therefore widely used in high-ratio IR zoom optical systems. This paper refers to the design of a mechanically compensated IR-zoom optical system, using 7 lenses, with a high zoom ratio, which meets the research direction of versatile thermal imaging equipment.

### 2 CALCULATION OF A ZOOM IR OPTICAL STRUCTURE

From the general theory of the mechanically compensated IR zoom system [1, 2, 3, 4, 5], the principal diagram of the mechanically compensated zoom system is selected including the following four main groups shown in Fig.1:



**Fig. 1** Diagram of the principle of positive compensation in the IR zoom optical system  
Source: authors.

In which,  $\varphi_1$  is the **front fixed group**,  $\varphi_2$  is the **variable/transform group**,  $\varphi_3$  is the **compensatory/offset group**, and  $\varphi_4$  is the **rear fixed group**. When the optical system is at the short focal position, the variable group  $\varphi_2$  close to the front fixed group  $\varphi_1$  and the positive compensation group  $\varphi_3$  is near the rear fixed group  $\varphi_4$ . When the system moves to the long focal position, the variable group  $\varphi_2$  shifts to the right and the compensatory group  $\varphi_3$  shifts in the opposite direction, forming the shortest distance  $d_{23m}$  between the variable group and the compensatory group [2, 3].

To determine the initial structure of the system, Gaussian optical calculations are used, and the focal lengths of the displacement groups (variable group and offset group)  $f'_2$  and  $f'_3$  are respectively preselected. The structure of the optical system diagram is taken from the long focal position as a basis for the calculation. Horizontal magnifications at the long focal position of the shifting groups are  $\beta_{2m}$  and  $\beta_{3m}$  respectively.

The following expression can be established from the optical figure in the diagram in Figure 1:

$$d_{23m} = -a_{3m} - (-a'_{2m}) = a'_{2m} - a_{3m}, \quad (1)$$

in which  $d_{23m}$  is the shortest distance between the variable group and the compensatory group (at the long focal position);  $a'_{2m}$  is the distance of the image point built across/through the variable group;  $a_{3m}$  is the object point distance to the offset group.

The horizontal magnifications of the displacement groups are calculated as follows.

$$\beta_{2m} = \frac{f'_2}{a_{2m} + f'_2} = -\frac{a'_{2m} - f'_2}{f'_2}, \quad (2)$$

$$\beta_{3m} = \frac{f'_3}{a_{3m} + f'_3} = -\frac{a'_{3m} - f'_3}{f'_3}. \quad (3)$$

Transforming Equations (2) and (3) to get:

$$a'_{2m} = f'_2(1 - \beta_{2m}), \quad (4)$$

$$a_{2m} = \frac{f'_2}{\beta_{2m}} - f'_2, \quad (5)$$

$$a_{3m} = \frac{f'_3}{\beta_{3m}} - f'_3. \quad (6)$$

Substituting equations (4) and (6) into (1) to get the distance:

$$d_{23} = f'_2(1 - \beta_{2m}) + f'_3(1 - \frac{1}{\beta_{3m}}). \quad (7)$$

Let us consider the optical system at the short focal position. According to optical construction, there are:

$$q = d_{12n} - d_{12m}, \quad (8)$$

$$q + a_{2m} = a_{2n}, \quad (9)$$

where  $q$  is the displacement of the group  $\varphi_2$ ;  $d_{12n}$  is the distance between group  $\varphi_1$  and group  $\varphi_2$  in a short focal position;  $d_{12m}$  is the distance between group  $\varphi_1$  and group  $\varphi_2$  in a long focal position;  $a_{2n}$  is object distance to group  $\varphi_2$  in a short focal position.

Using the formula in Eq. (2) for calculating the horizontal magnification of the variable group at the short focal position, we obtain:

$$a_{2n} = \frac{f'_2}{\beta_{2n}} - f'_2 \quad (10)$$

Substituting (5) and (10) into (9) and transforming to get:

$$\beta_{2n} = \frac{f'_2 \cdot \beta_{2m}}{q \cdot \beta_{2m} + f'_2}. \quad (11)$$

Equation (11) calculates the horizontal magnification of the point object through the variable group at the short focal position  $\beta_{2n}$  depending only on the amount of displacement  $q$ , the focal length  $f'_2$  and the horizontal magnification  $\beta_{2m}$  at the long focal position [2].

Find the magnification  $\beta_{3n}$  of the compensation group at the short focal position:

From the geometric relationship of the distance of object-image points through the zoom unit, it is easy to find the relationship between variable group magnification and offset group magnification when shifting from the long focal position to the short focal position (zoom equation) as follows [3].

$$f'_3 \left( \frac{1}{\beta_{3m}} + \beta_{3m} - \frac{1}{\beta_{3n}} - \beta_{3n} \right) + f'_2 \left( \frac{1}{\beta_{2m}} + \beta_{2m} - \frac{1}{\beta_{2n}} - \beta_{2n} \right) = 0. \quad (12)$$

Transforming equation (12) to find  $\beta_{3n}$ :

$$\beta_{3n}^2 - b \cdot \beta_{3n} + 1 = 0. \quad (13)$$

where  $b$  is the coefficient that has the value:

$$b = -\frac{f'_2}{f'_3} \left( \frac{1}{\beta_{2n}} - \frac{1}{\beta_{2m}} + \beta_{2n} - \beta_{2m} \right) + \left( \frac{1}{\beta_{3m}} + \beta_{3m} \right). \quad (14)$$

Solve the quadratic equation to find the value of  $\beta_{3n}$  according to the expression:

$$\beta_{3n} = \frac{b \pm \sqrt{b^2 - 4}}{2}. \quad (15)$$

This expression shows that, during zooming, corresponding to one magnification of the transform group, there will be two magnifications of the compensating group that satisfy the requirement for image surface stability.

Calculate the amount of displacement  $k$  of the compensation group:

From the diagram in Figure 1, it can be seen that the optical zoom objective system has a fixed image plane, which implies the following.

$$a'_{4n} = a'_{4m}. \quad (16)$$

Therefore, their conjugate segments must be equal:

$$a_{4n} = a_{4m}. \quad (17)$$

The amount of displacement  $k$  of the compensation group is equal to:

$$k = d_{34m} - d_{34n}. \quad (18)$$

Combining (17) with (18) we have:

$$k = (d_{34m} + a_{4m}) - (d_{34n} + a_{4n}) = a'_{3m} - a'_{3n}. \quad (19)$$

From the expression for calculating horizontal magnification according to Gaussian optics, the values of the image line segment built through the compensation group in the two configurations can be calculated as follows.

$$a'_{3m} = f'_3(1 - \beta_{3m}), \quad (20)$$

$$a'_{3n} = f'_3(1 - \beta_{3n}). \quad (21)$$

Substituting  $a'_{3m}$ ,  $a'_{3n}$  from (20) and (21) into the expression (19) to get:

$$k = f'_3(\beta_{3n} - \beta_{3m}). \quad (22)$$

The effective focal length of the optical system at the long focal position is

$$f'_m = f'_1 \cdot \beta_{2m} \cdot \beta_{3m} \cdot \beta_4, \quad (23)$$

where  $\beta_4$  is the horizontal magnification of the rear fixed lens group. Due to the requirement that the image plane does not change,  $\beta_4$  remains constant during the zooming process of the zoom objective system.

The general focal length of the optical system at the short focal position is:

$$f'_n = f'_1 \cdot \beta_{2n} \cdot \beta_{3n} \cdot \beta_4. \quad (24)$$

The zoom ratio is formed by the variable focal length of the zoom objective and is defined as  $\Gamma$ :

$$\Gamma = \frac{f'_m}{f'_n}. \quad (25)$$

Combining (23), (24), and (25) we have the following relationship of the product of magnifications of mobile components in two polar configurations:

$$\Gamma = \frac{\beta_{2m} \cdot \beta_{3m}}{\beta_{2n} \cdot \beta_{3n}}. \quad (26)$$

Equation (26) shows the relationship of the zoom ratio of the objective zoom optical system  $\Gamma$  to the product of the horizontal magnifications of the moving components in the two extreme configurations.

The distance between the variable group and the offset group at the short focal position is (see Figure 1):

$$d_{23n} = q + d_{23} + k. \quad (27)$$

Calculate the focal length  $f'_1$  according to the formula:

$$f'_1 = d_{12n} + a_{2n}. \quad (28)$$

Replace  $a_{2n}$  in Equation (10) into Equation (28) to get:

$$f'_1 = d_{12n} + f'_2 \left( \frac{1}{\beta_{2n}} - 1 \right). \quad (29)$$

Calculating the total length of the objective optical system: If the length of the objective optical system  $L$  is considered as the distance from the position of the fixed lens group in advance to the position of the image plane, then  $L$  can be calculated by the expression:

$$L = d_{12n} + q + d_{23m} + k + d_{34n} + a'_{4n}. \quad (30)$$

From the formulas built above, the initial structure of the optical system can be found [1, 2, 3].

### 3 DESIGN OF THE IR ZOOM SYSTEM

#### 3.1 Feature criteria of the optical zoom system to be designed

Choosing a set of design criteria for the IR zoom optical system based on the working distance of the equipment calculated according to Johnson's standard, combined with the selection of Flir's 640 x512 uncooled detector, which is commercially available, is valued as in Table 1.

From the set of indicators, it is necessary to design and allocate the component focal lengths and the distance between the components (groups) of the zoom objective to obtain the zoom ratio and maintain the overall length of the optical system. At the same time, no collision of the components occurs when moving.

**Tab. 1** The set of criteria and features of the optical zoom system to be designed

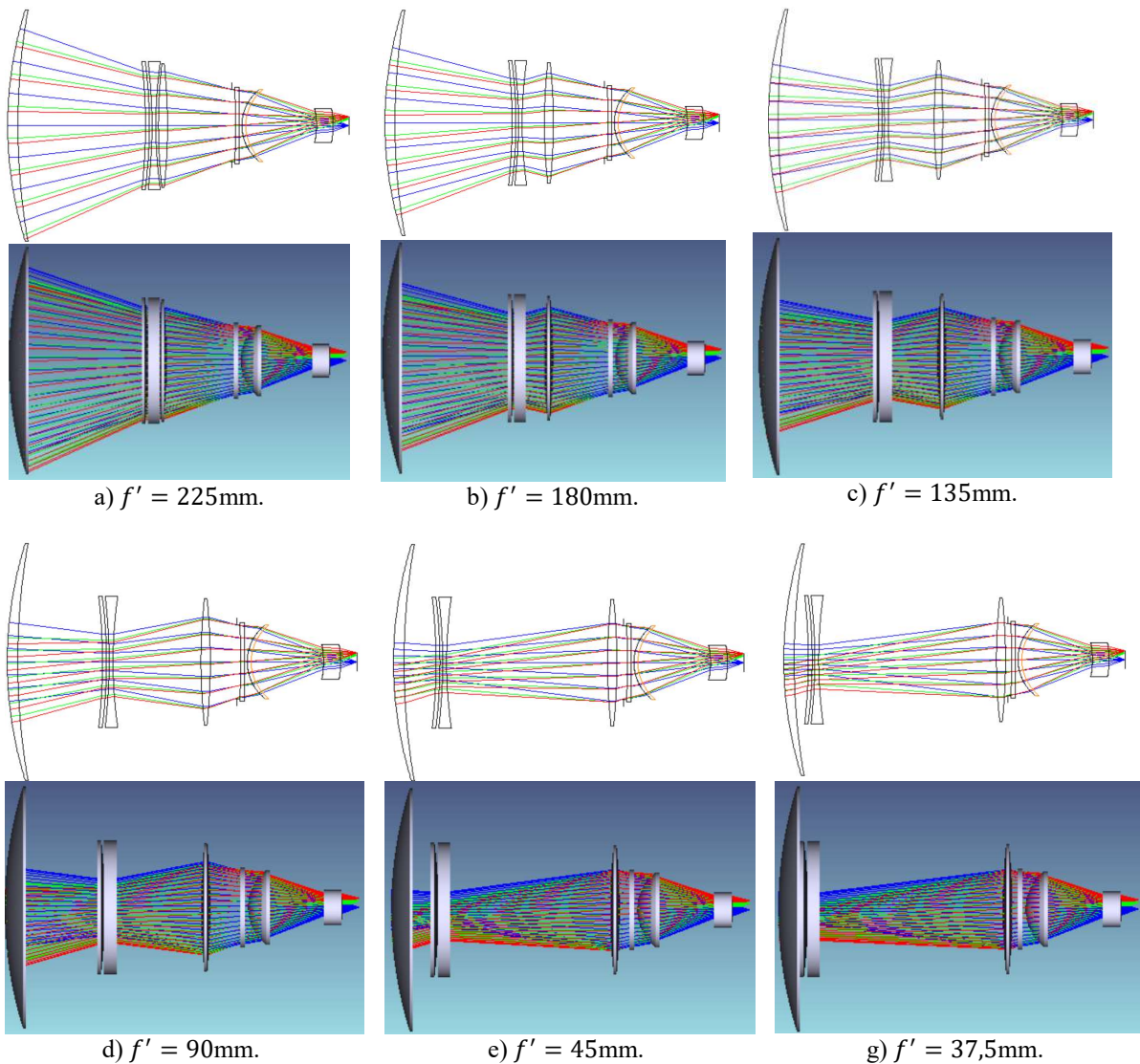
No.	Parameter	Value
1	Detector, pixel	640 x 512
2	The pitch of the detector pixels, $\mu m$	17
3	Working wavelength range, $\mu m$	8 ~ 12
4	Working focal range, mm	37,5~225
5	F/#	1,5
6	Zoom ratio, times	6
7	Lens length L, mm	$\leq 300$

Source: authors.

### 3.2 Design results

The distribution of this IR zoom system is: '+, '-', '+', and '+' in which the mobile group '-' performs zooming, and the movable group '+' performs image plane offset compensation. The movement of these two moving groups is ensured by a special cam mechanism.

To perform the optical system calculations, formulas from (1) to (30) are used. The optical materials Ge and ZnS, which are common and easy to machine and have different refractive indices and Abbe coefficients, are chosen. They help to eliminate axial chromatic aberration. The structure of the system at six different focal positions is shown in Figure 2.



**Fig. 2** Structure of the IR zoom optical system  
Source: authors.

The optical system consists of 7 lenses, of which 6 are made of Ge and 1 is made of ZnS. The fixed group  $\varphi_1$  is a single lens made of Ge, the variable group  $\varphi_2$ , which has negative power, consists of two lenses that perform the zoom, the third group  $\varphi_3$  is a positive lens that compensates for the image plane shift. The most complex rear fixation group  $\varphi_4$  consists of 3 lenses to eliminate residual aberrations from the front groups. The system has 3 even aspherical surfaces to eliminate higher-order aberrations. Applying the multi-configuration optimization in Zemax [6], the structure of the IR-zoom optical system is given in Table 2 with

the multi-configuration variable being the distances between groups  $\varphi_1, \varphi_2, \varphi_3, \varphi_4$ . During the design process, the sum of these three distances is constant and equal to 151,32 mm; the image plane is kept stable. The total length of the system is 265 mm and the constant F# is 1,5.

Table 3 shows the Lens Data Editor of Configuration 1 ( $f^*=225$  mm), in which the optical surfaces numbered 2, 10, and 14 are even aspheres to reduce aberrations. The system Stop on the ninth surface with a semi-diameter of 27,97 mm is unchanged.

**Tab. 2** Multi-configuration variable of the IR zoom optical system

Multi-Configuration Editor

Edit Solves Tools View Help

Active : 3/6	Config 1	Config 2	Config 3*	Config 4	Config 5	Config 6
1: APER	0	1.500	1.500 P	1.500 P	1.500 P	1.500 P
2: YFIE	2	4.930	4.930 P	4.930 P	4.930 P	4.930 P
3: YFIE	3	7.000	7.000 P	7.000 P	7.000 P	7.000 P
4: THIC	2	99.072 V	92.885 V	81.746 V	64.205 V	24.187 V
5: THIC	6	2.000 V	17.620 V	37.556 V	66.644 V	121.788 V
6: THIC	8	50.250 V	40.818 V	32.021 V	20.474 V	5.348 V

Source: authors.

**Tab. 3** The Lens Data Editor of Configuration 1 ( $f^*=225$  mm)

Lens Data Editor: Config 1/6

Edit Solves View Help

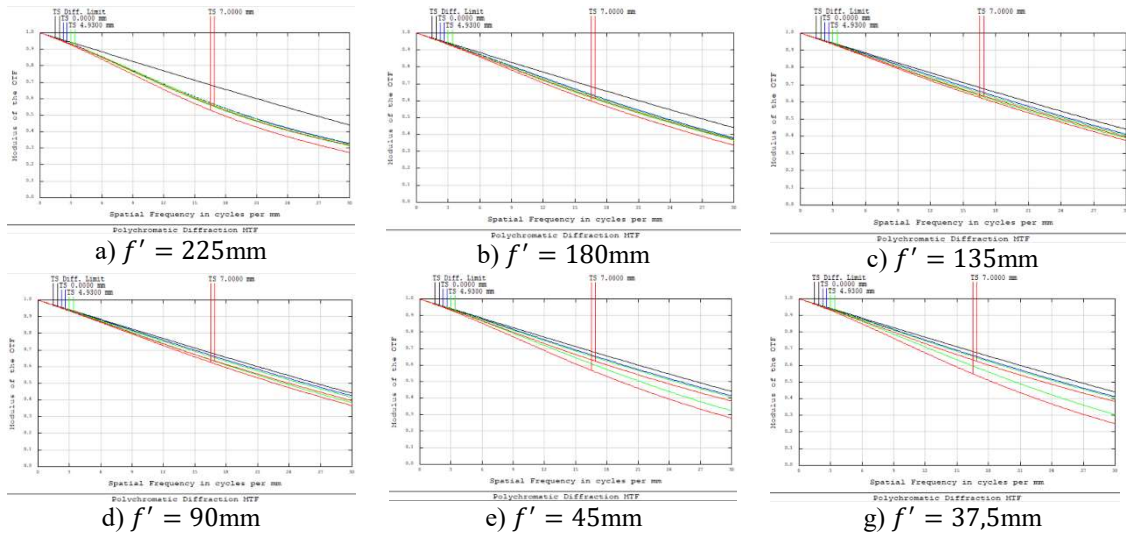
Surf:Type	Radius	Thickness	Glass	Semi-Diameter
OBJ Standard	Infinity	Infinity		Infinity
1* Standard	302.396 V	7.989 V	GERMANIUM	90.000 U
2* Even Asph..	525.492 V	99.072 V		90.000 U
3* Standard	-440.871 V	3.000 V	GERMANIUM	50.000 U
4* Standard	-397.279 V	2.051 V		50.000 U
5* Standard	-397.279 P	3.000 V	GERMANIUM	50.000 U
6* Standard	352.714 V	2.000 V		50.000 U
7* Standard	419.533 V	7.057 V	GERMANIUM	48.000 U
8* Standard	-469.091 V	50.250 V		48.000 U
STO Standard	Infinity	2.581 V		27.972
10* Even Asph..	-756.110 V	3.000 V	GERMANIUM	30.000 U
11* Standard	-3320.665 V	2.000 V		30.000 U
12* Standard	35.746 V	3.001 V	GERMANIUM	28.000 U
13* Standard	36.102 V	54.846 V		28.000 U
14* Even Asph..	-86.108 V	12.926 V	ZNS_BROAD	13.000 U
15* Standard	-73.990 V	12.227 V		13.000 U
IMA Standard	Infinity	-		7.046

Source: authors.

### 3.3 Evaluate image quality

MTF is one of the criteria to evaluate the quality of the optical system image designed. The MTF functions of the system in different focal

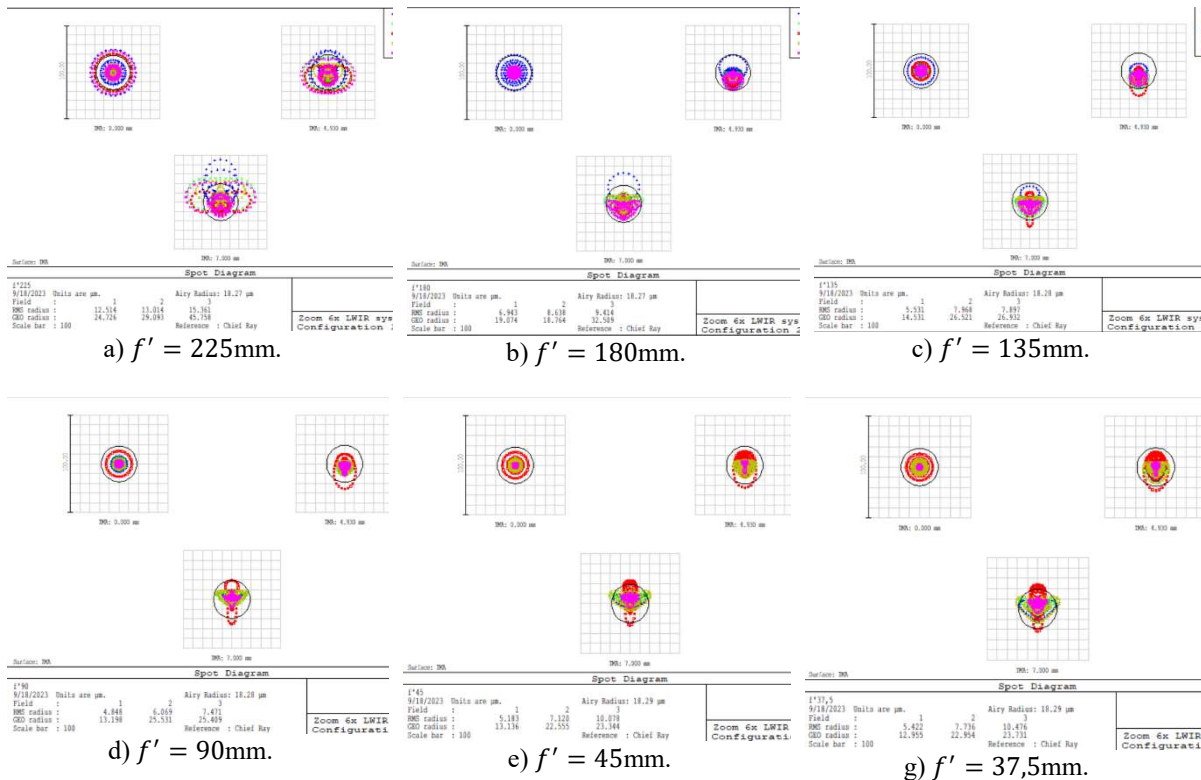
configurations are shown in Figures 3(a) to (g). The curves have a cutoff frequency of 30 lines/mm, with values above 0,25 and close to the diffraction limit, showing that the quality of the design system is acceptable [7].



**Fig. 3** MTF curve of the optical zoom system at different focal lengths  
Source: authors.

The spot diagram in the image plane of the optical system is also an indicator of quality. Figure 4 shows the spot diagram of 6 different focal positions of the designed zoom optical system. In Figure 4, it can be

seen that the RMS ray spot size at all positions is smaller than the pixel size, so the zoom system satisfies the image quality requirements of the detector.



**Fig. 4** Spot diagram at different focal positions  
Source: authors.

#### 4 CONCLUSION

An IR continuous-zoom optical system was designed in the LWIR range with a 6x zoom ratio operating with a 640x512 pixel uncooled detector. Evaluating the quality of the MTF function and the spot diagrams shows that the zoom system is quite good quality. Zoom optical system with continuously variable focal length from 37,5 mm to 225 mm, constant F/#1.5, compact structure, suitable for target positioning and search applications in the LWIR waveband.

The design of the infrared zoom optical system needs to continue in the direction of uniformly increasing image quality throughout the entire zoom range, paying attention to the feasibility of the motion curve of the compensation cam mechanism and further expanding the zoom ratio, meeting the increasing requirements for observing and tracking thermal targets.

#### References

- [1] MU Da, DU Yu-nan, Mi Shi-long and GUO Yan-chi. *Design of 10x uncooled thermal infrared zoom optical system*, Proc. of SPIE Vol. 8907.
- [2] YAN Jing, SUN Quan, LIU Ying, ZHOU Hao, HUAN Ke-wei, SHI Xiao-guang. *High ratio long-way infrared continuous zoom system*, Proc. of SPIE Vol. 8907.
- [3] Tao ChunKan. *Varifocal differential equation theory of zoom lens*. 168/SPIE Vol.2539.
- [4] AD Clark. *Zoom lenses*. Adam Hilger, 1973.
- [5] Allen Mann. *Infrared optics and zoom lenses. Volume TT83*, 2009. Available at: <https://doi.org/10.1117/3.829008>.
- [6] Zemax 13 Premium Programme. 2014.
- [7] Available at: <https://www.ophiiopt.com/infrared/>

Chi Toan **DANG**  
University of Defence  
Kounicova 65  
662 10 Brno  
Czech Republic  
E-mail: [chitoan.dang@unob.cz](mailto:chitoan.dang@unob.cz)

Dipl. Eng. Vratislav **KREHEL**  
Armed Forces Academy of General M. R. Štefánik  
Demänová 393  
031 01 Liptovský Mikuláš  
Slovak Republic  
E-mail: [vratislav.krehel@aos.sk](mailto:vratislav.krehel@aos.sk)

Capt. Dipl. Eng. Michal **MOZOLA**  
Armed Forces Academy of General M. R. Štefánik  
Demänová 393  
031 01 Liptovský Mikuláš  
Slovak Republic  
E-mail: [michal.mozola@aos.sk](mailto:michal.mozola@aos.sk)

**Chi Toan DANG** was born in 1978. He graduated from Le Qui Don University of Technology, Hanoi, Vietnam in 2002 as an optical instrument engineer. He graduated with a Master's degree from Le Qui Don Technical University, Hanoi, Vietnam in 2018, majoring in optoelectronics. He worked in the optoelectronics factory, under the General Department of Defence Industry of Vietnam (2002-2011). Then he worked at the Weapons Institute of Vietnam, General Department of Defence Industry of Vietnam (since 2011). Currently, he is working as a doctoral student at the University of Defence, Brno, Czech Republic. Participated in optical processing technology, total installation of night vision devices, measurement, design of night vision lenses, and infrared lenses.

**Vratislav KREHEL** was born in Liptovský Mikuláš, Slovakia in 1972. He received his M. Sc (Eng.) at the Military Academy in Liptovský Mikuláš in 2003. He started his dissertation studies in 2021. His research interests are focused on optimization of sniper weapons fire mode. He is currently working as an assistant professor at the Department of Mechanical Engineering, Armed Forces Academy of General M. R. Štefánik in Liptovský Mikuláš.

**Michal MOZOLA** was born in Krupina, Slovakia in 1988. He received his M. Sc (Eng.) at the Armed Forces Academy in Liptovský Mikuláš in 2017. He started his dissertation studies in 2022. His research interests are focused on the optimisation of automatic weapon fire modes. He is currently working as an assistant professor at the Department of Mechanical Engineering, Armed Forces Academy of General M. R. Štefánik in Liptovský Mikuláš.